

$$5) \quad 16x^2 + 9y^2 - 64x - 54y + 1 = 0$$

$$16x^2 - 64x + 9y^2 - 54y + 1 = 0$$

$$16(x^2 - 4x) + 9(y^2 - 6y) + 1 = 0$$

$$\underbrace{16(x^2 - 4x + 4)}_{16(x-2)^2} + \underbrace{9(y^2 - 6y + 9)}_{9(y-3)^2} + 1 = 0$$

$$16(x-2)^2 + 9(y-3)^2 + 1 = 64 + 81$$

$$16(x-2)^2 + 9(y-3)^2 = 144$$

$$\frac{(x-2)^2}{9} + \frac{(y-3)^2}{16} = 1$$

Ellipse: $a=4$, $b=3$, $\Rightarrow c=\sqrt{7}$ Vertical Axis

center: $(h, k) = (2, 3)$

vertices: $(h, k \pm a) : (2, 7)(2, -1)$

foci: $(2, 3 \pm \sqrt{7})$

